

## SYNTHESIS OF POLARIZATION FOR PLANAR ARRAYS : AN EXAMPLE.

FLEURIAULT J.M., FUCHS J.J., TERRET C.

IRISA (URA CNRS 227) and Laboratoire "Structures rayonnantes" (URA CNRS 834).  
Campus de Beaulieu. 35042 RENNES Cedex.FRANCE.

### Abstract :

This paper deals with antenna synthesis in the case of an array of N elements. The use of a variational method described in [1] allows us to synthesize the complex weights to be applied to the elements in order to obtain a linear polarization for the total electric field and to meet a desired power pattern.

An example of this synthesis technique will be given in the case of an uniform linear array of N dipoles, the orientation of each being fixed randomly. A linear polarization along  $\vec{u}_\theta$  is desired in the plane  $\varphi = 0^\circ$  of the spherical coordinates. The power pattern will be directional.

### Radiation intensity of one element :

The electric field emitted by a dipole (with length 2.l), fed with a current  $\vec{I} = I_m \cdot \sin(\frac{2\pi}{\lambda} \cdot (l - |x|)) \cdot \vec{u}_x$  can be found using the expression :

$$\vec{d}(\theta, \varphi) = A_E(\theta, \varphi) \cdot \cos(\varphi) \cdot \vec{u}_\theta - A_H(\theta, \varphi) \cdot \sin(\varphi) \cdot \vec{u}_\varphi \quad (1)$$

$$\begin{cases} A_E &= \frac{1}{(\cos(\theta) \cdot \cos(\varphi)^2 - 1)} \cdot (\cos(\frac{2\pi}{\lambda} \cdot l) - \cos(\frac{2\pi}{\lambda} \cdot \sin(\theta) \cdot \cos(\varphi))) \\ A_H &= A_E \cdot \cos(\theta) \end{cases}$$

If the orientation of the element is repared by an angle  $\alpha_1$ , this expression becomes :

$$\vec{d}^1(\theta, \varphi) = d_\theta^1(\theta, \varphi - \alpha_1) \cdot \vec{u}_\theta + d_\varphi^1(\theta, \varphi - \alpha_1) \cdot \vec{u}_\varphi \quad (2)$$

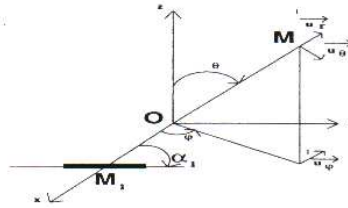


FIG. 1 -

The dipole is described by its position  $M_1$  and its angle  $\alpha_1$  (see figure 1)

### Array of N elements :

For an array of N elements, described by their positions (with respect to a fixed point O :  $O\vec{M}_p$ ) and by their orientation (with respect to the Ox axis :  $\alpha_p$ ), the radiation intensity can be written as :

$$D(\theta, \varphi) = \left| \sum_{p=1}^N d_\theta^p(\theta, \varphi) \cdot I_p \cdot \exp\left(\frac{2 \cdot i \cdot \pi}{\lambda} \cdot O\vec{M}_p \cdot \vec{u}_r\right) \right|^2 + \left| \sum_{p=1}^N d_\varphi^p(\theta, \varphi) \cdot I_p \cdot \exp\left(\frac{2 \cdot i \cdot \pi}{\lambda} \cdot O\vec{M}_p \cdot \vec{u}_r\right) \right|^2 \quad (3)$$

where  $d_\theta^p$  and  $d_\varphi^p$  are given by equations (1) and (2).

### Synthesis technique :

With a variational technique described in [1], one can minimize :

- the difference between the desired pattern and  $D(\theta, \varphi)$  for a set of spherical angles.
- the cross-polarization in a desired plane.

so that the polarization is along a desired vector.

An example of N=32 half-wavelength dipoles will be presented and several other examples will be given during the presentation.

For the array of 32 dipoles, the total electric field is forced to follow the vector  $\vec{u}_\theta$  in the plane  $\varphi=0^\circ$ .

In the main lobe, the cross polarization is 20dB below the modulus of the coefficient of  $\vec{u}_\theta$ .

In the side lobes, the modulus of the total electric field is less than -30dB for all the angles  $\theta$ . The angles  $\alpha_p$  are randomized numbers between  $-\pi/4$  and  $+\pi/4$ .

[1] J.M FLEURIAULT, P.GONNET, J.J FUCHS, C.TERRET "Antenna pattern synthesis for conformal arrays. Comparison of two different methods.", *PIERS 1995 conference*, SEATTLE, July 1995.